

Duration : 2h — All documents authorized

Python programming — (8 points)

1– «Hamming distance» is a **metric** for comparing two binary data strings. While comparing two binary strings of equal length, Hamming distance is the **number of bit positions** in which the two bits are **different**.

The Hamming distance between two strings, a and b is denoted as $d(a, b)$.

In order to calculate $d(a, b)$ between two strings, and , we perform their XOR operation, $a \oplus b$, and then count the total number of 1s in the resultant string.

Example : Suppose there are two strings 1101 1001 and 1001 1101 :

- ▷ $11011001 \oplus 10011101 = 01000100$, where \oplus is the «xor» ;
- ▷ the result is 0100 0100 containing two 1s, the Hamming distance is 2.
- ⇒ $d(11011001, 10011101) = 2$

In a set of strings of **equal lengths**, the **minimum Hamming distance** is the **smallest** Hamming distance between all possible pairs of strings in that set.

a. Let the set of binary strings be : 1110010, 1001001, 1001111, 0101100 (1pt)
Compute the minimum Hamming distance for this set.

b. In Python, the «xor» operation is denoted ^ and is used according to : (1pt)

```
xterm
>>> 12^3
15
```

Explain how, in Python, we could compute a «xor» between two binary strings.

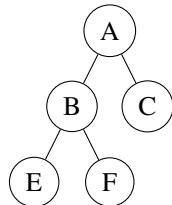
c. Write a Python function that takes two binary strings as arguments and return the Hamming distance (2pts) between these two string.

d. Write a Python program that uses the previous function to compute the « minimum Hamming distance » (2pts) for a set of binary strings given as a list.

e. Write a Python program that, giving a random binary string, return the nearest binary string from a set (2pts) S of known binary strings (the random binary string doesn't belong necessary to the set S).

2– We represent a **binary tree** as a list of embedded lists :

3pts node = [head, child1, child2] (an empty node is given by an empty list).



```
1 arbre = ['A',
2         ['B',
3          ['E', [], []],
4          ['F', [], []]
5         ], # fin de B
6         ['C',
7          [],
8          []
9         ] # fin de C
10      ]
```

Write a Python program that display each node of the tree.

Unix — (2 points)

3– a. For a 64bits computer under Linux, the size of page is 4096 bytes : how much pages do we get ? (1pt)

2pts b. Does it matter if the starting address of a program in the central memory is shifted from one byte before (1pt) its execution by the processor ?
Explain what happens.



■ ■ ■ **Networking — (5 points)**

- 4– a. We want to design a **TCP server** that receives a value denoted in hexadecimal and return a value expressed as an integer. (1pt)
5pts What information must be **shared** with the client using this server ?
- b. Write a Python program acting as a TCP server that **for each received connection** performs the conversion from hexadecimal to integer (only one conversion for one connection). (3pts)
- c. If we want to extend the capabilities of the server to perform the **reverse operation** « *integer* \Rightarrow *hexadecimal* », how to proceed ? (1pt)